

## Inverse of a Matrix

Name: \_\_\_\_\_

Multiply to determine if the two matrices are inverses of each other.

$$1) \begin{bmatrix} 0 & 1 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} 1 & -1 \\ -1 & 0 \end{bmatrix}$$

Find the inverse of each matrix if it exists. Complete #'s 2-5 by hand.

$$2) \begin{bmatrix} 6 & 2 \\ -1 & 5 \end{bmatrix}$$

$$3) \begin{bmatrix} 4 & 0 \\ 7 & 5 \end{bmatrix}$$

$$4) \begin{bmatrix} 2 & 12 \\ 1 & 6 \end{bmatrix}$$

$$5) \begin{bmatrix} 3 & 0 \\ 1 & -2 \end{bmatrix}$$

6)  $B$  is the inverse of  $\begin{bmatrix} -1 & 6 \\ 4 & 3 \end{bmatrix}$ . What is entry  $b_{11}$ ?

Solve the following system of equations using a matrix equation.

$$7) \begin{cases} x - y = 5 \\ 2x - y = 6 \end{cases}$$

**Write and solve the matrix equation that represents the system.** *Identify your variables.*

8) A game show host says that he has \$5000 in \$50 bills and \$100 bills and he will give you the \$5000 if you can tell him how many of each type of bill he has. He gives you a hint that he has 73 bills in all. How many of each bill does the game show host have?

|       |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|-------|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 0     | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 |
| Space | A | B | C | D | E | F | G | H | I | J  | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  |

9) The matrix  $\begin{bmatrix} 1 & -2 & 3 & 0 \\ 2 & 4 & -2 & -3 \\ 1 & -1 & 2 & 1 \\ -2 & -1 & 0 & 1 \end{bmatrix}$  was used to encrypt a message sent by Morpheus to Neo in the Matrix movie. The

encoded message Neo received was the matrix:  $\begin{bmatrix} 24 & 32 & 19 & -4 \\ 24 & 13 & -38 & -28 \\ 43 & 38 & 26 & 10 \\ -35 & -19 & 4 & 10 \end{bmatrix}$ . Decode this message.

10) Neo used the matrix  $\begin{bmatrix} -1 & 3 \\ 4 & -2 \end{bmatrix}$  to send the encrypted message  $\begin{bmatrix} 15 & 15 & -1 & 32 & 42 & -5 \\ 20 & -10 & 4 & 22 & -28 & 70 \end{bmatrix}$ . What did Neo's message say?