

# Calculus Section 2.2 Basic Differentiation Rules

- Find the derivative of a function using the constant rule
- Find the derivative of a function using the power rule
- Find the derivative of the sine and cosine functions.

Homework: Page 114 #'s 3-22, 31, 40, 57, 61, 63

You do not have to use the limit definition of the derivative to find the derivative of a function because there is a shortcut.

## Derivative Constant Rule and Power Rule

The derivative of a constant number is zero. This is because the graph of a constant is a horizontal line. Therefore, the slope of a constant must be zero.

The derivative of a function with  $x$  raised to a power  $f(x) = x^n$  is  $f'(x) = nx^{n-1}$

Examples)

$$1) f(x) = x^5 \\ f'(x) = 5x^4$$

$$2) f(x) = \frac{1}{x^2} \\ f(x) = x^{-2} \\ f'(x) = -2x^{-3} \\ f'(x) = \frac{-2}{x^3}$$

$$3) f(x) = \sqrt[3]{x^2} \\ f(x) = x^{2/3} \\ f'(x) = \frac{2}{3}x^{-1/3} \\ f'(x) = \frac{2}{3x^{1/3}}$$

## The Constant Multiple Rule

If  $f$  is a differentiable function and  $c$  is a real number, then  $cf$  is also differentiable:

$$f(x) = [cf(x)] \text{ then } f'(x) = [cf'(x)]$$

Examples)

$$1) f(x) = 3x^2 \\ f'(x) = 6x$$

$$2) f(x) = \frac{2}{x} \\ f(x) = 2x^{-1} \\ f'(x) = -2x^{-2} \\ f'(x) = \frac{-2}{x^2}$$

$$3) f(x) = 3\sqrt[5]{x^3} \\ f(x) = 3x^{3/5} \\ f'(x) = \frac{9}{5}x^{-2/5} \\ f'(x) = \frac{9}{5x^{2/5}}$$

## Sum and Difference Rule

If both  $f$  and  $g$  are differentiable, then the sum or difference of  $f$  and  $g$  is differentiable as well.

$$f(x) = [f(x) \pm g(x)] \text{ then } f'(x) = [f'(x) \pm g'(x)]$$

Examples)

$$1) f(x) = x^3 + x^2 - 2$$

$$f'(x) = 3x^2 + 2x$$

$$2) f(x) = 3x^5 - 2x^3 + \frac{1}{x}$$

$$f'(x) = 15x^4 - 6x^2 - \frac{1}{x^2}$$

### Derivative of Sine and Cosine Functions

$$\frac{d}{dx}[\sin x] = \cos x$$

$$\frac{d}{dx}[\cos x] = -\sin x$$

Examples)

$$1) f(x) = 2 \sin x$$

$$f'(x) = 2 \cos x$$

$$2) f(x) = \frac{1}{2} \sin x$$

$$f'(x) = \frac{1}{2} \cos x$$

$$3) f(x) = x + \cos x$$

$$f'(x) = 1 - \sin x$$

### Horizontal Tangent Line

Horizontal tangent lines have many applications in calculus. You can find where a function has a horizontal tangent line

by taking the derivative of the function and setting it equal to zero.

For what values of  $x$  do the following functions have a horizontal tangent line?

$$1) f(x) = 3x^2 - 2x + 1$$

$$f'(x) = 6x - 2$$

$$0 = 6x - 2$$

$$6x = 2$$

$$x = \frac{1}{3}$$

$$2) f(x) = -\cos(x)$$

$$f'(x) = \sin x$$

$$0 = \sin x$$

$$x = 0, \pi, 2\pi, \dots$$