1)

x	f(x)	f'(x)	g(x)	g'(x)
1	6	4	2	5
2	9	2	3	1
3	10	- 4	4	2
4	-1	3	6	7

The functions f and g are differentiable for all real numbers, and g is strictly increasing. The table above gives values of the functions and their first derivatives at selected values of x. The function h is given by h(x) = f(g(x)) - 6.

- (a) Explain why there must be a value r for 1 < r < 3 such that h(r) = −5.</p>
- (b) Explain why there must be a value c for 1 < c < 3 such that h'(c) = −5.</p>

2) 1998 #91 (AB but suitable for BC) - Calc OK:Let f be a function that is differentiable on the open interval (1, 10). If f(2) = -5, f(5) = 5, and f(9) = -5, which of the following must be true?

I. f has at least 2 zeros. II. The graph of f has at least one horizontal tangent. III. For some c, 2 < c < 5, f(c) = 3.

- a. None c. I and II only e. I, II and III
- b. I only d. I and III only
- 3) 2003 #80 (AB but suitable for BC) Calc OK: The function f is continuous for -2 ≤ x ≤ 1 and differentiable for -2 < x < 1. If f(-2) = -5 and f(1) = 4, which of the following statements could be false?</p>
 - a. There exists c, where -2 < c < 1, such that f(c) = 0.
 - b. There exists c, where -2 < c < 1, such that f'(c) = 0.
 - c. There exists c, where -2 < c < 1, such that f(c) = 3.
 - d. There exists c, where -2 < c < 1, such that f'(c) = 3.
 - e. There exists c, where $-2 \le c \le 1$ such that $f(c) \ge f(x)$ for all x on the closed interval $-2 \le x \le 1$.

4) 1998 #4 (AB but suitable for BC) - No Calc: If f is continuous for a ≤ x ≤ b and differentiable for a < x < b, which of the following could be false?</p>

a.
$$f'(c) = \frac{f(b) - f(a)}{b - a}$$
 for some c such that $a < c < b$.

- b. f'(c) = 0 for some c such that a < c < b.
- c. f has a minimum value on $a \le x \le b$.
- d. f has a maximum value on $a \le x \le b$.

5) The value of c guaranteed to exist by the Mean Value Theorem for $V(x) = x^2$ in the interval [0, 3] is

A) 1 B) 2 C) 3/2 D) 1/2 E) None of these

6) If P(x) is continuous in [k,m] and differentiable in (k, m), then the Mean Value Theorem states that there is a point a between k and m such that

A)
$$\frac{P(k) - P(m)}{m - k} = P'(a)$$

B)
$$P'(a)(k - m) = P(k) - P(m)$$

C)
$$\frac{m - k}{P(m) - P(k)} = a$$

D)
$$\frac{m - k}{P(m) - P(k)} = P'(a)$$

7) The Mean Value Theorem does not apply to f(x) = |x - 3| on [1,4] because

- A) f(x) is not continuous on [1, 4]
- B) f(x) is not differentiable on (1, 4)
- C) $f(1) \neq f(4)$
- D) f(1) > f(4)
- 8) Train A runs back and forth on an east-west section of railroad track. Train A's velocity, measured in meters per minute, is given by a differentiable function v_A(t), where time t is measured in minutes. Selected values for v_A(t) are given in the table above.

t (minutes)	0	2	5	8	12
$v_A(t)$ (meters/minute)	0	100	40	-120	-150

- (a) Find the average acceleration of train A over the interval $2 \le t \le 8$.
- (b) Do the data in the table support the conclusion that train A's velocity is −100 meters per minute at some time t with 5 < t < 8 ? Give a reason for your answer.</p>

E) None of these