

7.1 Area Between Two Curves

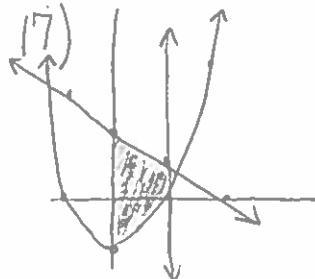
Pg. 442 #'s 1-4, 17, 19, 23, 71

$$1) \int_0^6 ((0) - (x^2 - 6x)) dx$$

$$2) \int_{-2}^2 ((2x+5) - (x^2 + 2x + 1)) dx$$

$$3) \int_0^3 ((-x^2 + 2x + 3) - (x^2 - 4x + 3)) dx$$

$$4) \int_0^1 ((x^2) - (x^3)) dx$$



$$\int_0^6 ((0) - (x^2 - 6x)) dx$$

$$\int_0^1 (-x^2 + 2x + 3) dx$$

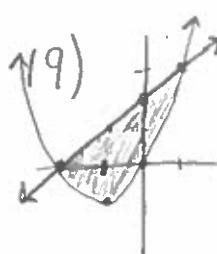
$$\int_0^1 (-x^2 - x + 3) dx$$

$$\left(-\frac{1}{3}x^3 - \frac{1}{2}x^2 + 3x \right) \Big|_0^1$$

$$\left(-\frac{1}{3} - \frac{1}{2} + 3 \right) - (0)$$

$$-\frac{2}{6} - \frac{3}{6} + \frac{18}{6}$$

$$\boxed{\frac{13}{6}}$$



$$17) \int_{-2}^2 ((2x+5) - (x^2 + 2x + 1)) dx$$

$$\int_{-2}^1 (-x^2 - x + 2) dx$$

$$\left(-\frac{1}{3}x^3 - \frac{1}{2}x^2 + 2x \right) \Big|_{-2}^1$$

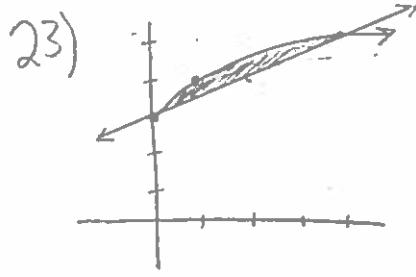
$$\left(-\frac{1}{3} - \frac{1}{2} + 2 \right) - \left(\frac{8}{3} - 2 - 4 \right)$$

$$-\frac{1}{3} - \frac{1}{2} + 2 - \frac{8}{3} + 2 + 4$$

$$-\frac{9}{3} - \frac{1}{2} + 8$$

$$-3 - \frac{1}{2} + 8$$

$$\boxed{4.5}$$



$$\int_0^4 \left((\sqrt{x} + 3) - \left(\frac{1}{2}x + 3\right) \right) dx$$

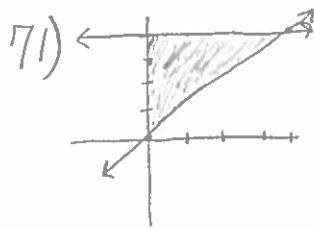
$$\int_0^4 \left(x^{1/2} - \frac{1}{2}x \right) dx$$

$$\left(\frac{2}{3}x^{3/2} - \frac{1}{4}x^2 \right) \Big|_0^4$$

$$\left(\frac{2}{3}(8) - \frac{1}{4}(16) \right) - (0)$$

$$\frac{16}{3} - 4$$

$$\boxed{\frac{4}{3}}$$



$$\int_0^4 ((4) - (x)) dx$$

$$\int_0^4 (4-x) dx$$

$$(4x - \frac{1}{2}x^2) \Big|_0^4$$

$$(16 - 8) - (0)$$

8

$$8 \div 2 = 4$$

$$\int_0^a (4-x) dx = 4$$

$$(4x - \frac{1}{2}x^2) \Big|_0^a = 4$$

$$(4a - \frac{1}{2}a^2) - (0) = 4$$

$$4a - \frac{1}{2}a^2 = 4$$

$$8a - a^2 = 8$$

$$a^2 - 8a + 8 = 0$$

$$\frac{8 \pm \sqrt{8^2 - 4(1)(8)}}{2(1)}$$

$$\frac{8 \pm \sqrt{64 - 32}}{2}$$

$$\frac{8 \pm \sqrt{32}}{2}$$

$$\frac{8 \pm 2\sqrt{2}}{2}$$

$$4 \pm \sqrt{2}$$

$$4 + \sqrt{2}$$

$$\boxed{4 - \sqrt{2}}$$