

Practice AP Questions 2.1-2.4

Name: _____

1) If $f(x) = \sqrt{4 \sin x + 2}$, then $f'(0) =$

- (A) -2 (B) 0 (C) 1 (D) $\sqrt{2}/2$ (E) $\sqrt{2}$

2) A particle moves along the x-axis in such a way that its position at time t is given by $x(t) = \frac{1-t}{1+t}$. What is the acceleration of the particle at time $t=0$?

- (A) -4
(B) -2
(C) -3/5
(D) 2
(E) 4

3) Let f be the function given by $f(x) = \tan x$ and let g be the function given by $g(x) = x^2$. At what value of x in the interval $0 \leq x \leq \pi$ do the graphs of f and g have parallel tangent lines?

- (A) 0
(B) 0.660
(C) 2.083
(D) 2.194
(E) 2.207

4) Two functions $f(x)$ and $g(x)$ are differentiable. If $h(x) = x^2g(x) - f(3x + 1)$, determine the value of $h'(x)$.

- (A) $2xg'(x) - 3f'(3x + 1)$
(B) $2xg'(x) - f'(3)$
(C) $x^2g'(x) + 2xg(x) - f'(3x + 1)$
(D) $x^2g'(x) + 2xg(x) - 3f'(3x + 1)$
(E) $x^2g'(x) - f'(3x + 1)$

5) Let f and g be differentiable functions such that

$$f(1) = 4, g(1) = 3, f'(3) = -5$$

$$f'(1) = -4, g'(1) = -3, g'(3) = 2$$

If $h(x) = f(g(x))$, then $h'(1) =$

(A) -9

(B) 15

(C) 0

(D) -5

(E) -12

6) If $f(x) = (2 + 3x)^4$, then the fourth derivative of f is

(A) 0

(B) $4!(3)$

(C) $4!(3^4)$

(D) $4!(3^5)$

(E) $4!(2 + 3x)$

7) The $\lim_{h \rightarrow 0} \frac{|x+h| - |x|}{h}$ at $x = 3$ is

(A) -1

(B) 0

(C) 1

(D) 3

(E) nonexistent

8) If $y = 7$ is a horizontal asymptote of a rational function f , then which of the following must be true?

(A) $\lim_{x \rightarrow 7} f(x) = \infty$

(B) $\lim_{x \rightarrow -\infty} f(x) = -7$

(C) $\lim_{x \rightarrow 0} f(x) = 7$

(D) $\lim_{x \rightarrow 7} f(x) = 0$

(E) $\lim_{x \rightarrow \infty} f(x) = 7$

9) Let $f(x)$ be a continuous and differentiable function. The table below gives the values of $f(x)$ and $f'(x)$, the derivative of

$f(x)$, at several values. If $g(x) = \frac{1}{f(x)}$, what is the value of $g'(2)$?

(A) -1/8

(B) 0

(C) 1/16

(D) 1/64

(E) 16

x	1	2	3	4
$f(x)$	-3	-8	-9	0
$f'(x)$	-5	-4	3	16

10) If $f(x) = \cos^2(x)$, then $f''(\pi) =$

- (A) -2 (B) 0 (C) 1 (D) 2 (E) 2π

11) Two particles leave the origin at the same time and move along the y -axis with their respective positions determined by the functions $y_1 = \cos 2t$ and $y_2 = 4\sin t$ for $0 < t < 6$. For how many values of t do the particles have the same acceleration?

- (A) 0 (B) 1 (C) 2 (D) 3 (E) 4

12) Evaluate $\lim_{h \rightarrow 0} \frac{5\left(\frac{1}{2} + h\right)^4 - 5\left(\frac{1}{2}\right)^4}{h}$.

- (A) $5/2$ (B) $5/16$ (C) 40 (D) 160 (E) The limit DNE

13) If f is continuous on $[2, 6]$, with $f(2) = 20$ and $f(6) = 10$, then the Intermediate Value Theorem says which of the following is true?

- I. $f(x) = 25$ does not have a solution on $[2, 6]$
- II. $f(x) = 17$ has a solution on $[2, 6]$
- III. $f(x) = 0$ has a solution on $[2, 6]$

- (A) I only (B) II only (C) III only (D) I and II only (E) I, II, and III