## AP Questions Chapter 7

1) For the figure to the right, the area of the shaded region is
(A) $14 / 3$
(B) $16 / 3$
(C) $28 / 3$
(D) $32 / 3$
(E) $65 / 3$

2) If, for all real numbers $x, f(x)=g(x)+5$, then on any interval $[a, b]$ the area of the region between the graphs of $f(x)$ and $\mathrm{g}(\mathrm{x})$ is
(A) 5
(B) $5 a+5 b$
(C) $5 b-5 a$
(D) $5 a-5 b$
(E) 5 ab
3) The region in the first quadrant enclosed by the graphs $y=x$ and $y=2 \sin x$ is revolved about the $x$-axis. The volume of the solid generated is
(A) 1.895
(B) 2.126
(C) 5.811
(D) 6.678
(E) 13.355
4) The area of the region between the graph of $y=3 x^{2}+2 x$ and the $x$-axis from $x=1$ to $x=3$ is
(A) 36
(B) 34
(C) 31
(D) 26
(E) 12
5) The base of a solid is the region in the first quadrant bounded by the line $x+2 y=4$ and the coordinate axes. What is the volume of the solid if every cross section perpendicular to the $x$-axis is a semicircle?
(A) $\frac{2 \pi}{3}$
(B) $\frac{4 \pi}{3}$
(C) $\frac{8 \pi}{3}$
(D) $\frac{32 \pi}{3}$
(E) $\frac{64 \pi}{3}$
6) The region in the first quadrant enclosed by the $x$-axis, the line $x=\pi$, and the curve $y=\cos (\cos (x))$ is rotated about the $x$-axis. What is the volume of the solid generated?
(A) 1.921
(B) 3.782
(C) 6.040
(D) 8.130
(E) 23.781
7) The region bounded by the $x$-axis and the part of the graph of $y=\cos x$ between $x=0$ and $x=\pi / 2$ is divided into two regions by the line $x=c$. If the area of the region for $0 \leq x \leq c$ is equal to the area of the region for $c \leq x \leq \pi / 2$, the $c$ must be
(A) $\frac{\pi}{4}$
(B) $\frac{\pi}{6}$
(C) $\frac{\pi}{3}$
(D) $\frac{2 \pi}{9}$
(E) $\frac{5 \pi}{18}$
8) The region enclosed by the line $x+y=1$ and the coordinate axes is rotated about the line $y=-1$. What is the volume of the solid generated?
(A) $\frac{17 \pi}{2}$
(B) $\frac{12 \pi}{4}$
(C) $\frac{2 \pi}{3}$
(D) $\frac{3 \pi}{4}$
(E) $\frac{4 \pi}{3}$
9) 2015 Question \#2 Calculator

Let $f$ and $g$ be the functions defined by $f(x)=1+x+e^{x^{2}-2 x}$ and $g(x)=x^{4}-6.5 x^{2}+6 x+2$. Let $R$ and $S$ be the two regions enclosed by the graphs of $f$ and $g$ shown in the figure above.
(a) Find the sum of the areas of regions $R$ and $S$.
(b) Region $S$ is the base of a solid whose cross sections perpendicular to the $x$-axis are squares. Find the volume of the solid.
(c) Let $h$ be the vertical distance between the graphs of $f$ and $g$ in region $S$. Find the rate at which $h$ changes with respect to $x$ when $x=1.8$.

10) 2014 Question \#2 Calculator

Let $R$ be the region enclosed by the graph of $f(x)=x^{4}-2.3 x^{3}+4$ and the horizontal line $y=4$, as shown in the figure above.
(a) Find the volume of the solid generated when $R$ is rotated about the horizontal line $y=-2$.
(b) Region $R$ is the base of a solid. For this solid, each cross section perpendicular to the $x$-axis is an isosceles right triangle with a leg in $R$. Find the volume of the solid.
(c) The vertical line $x=k$ divides $R$ into two regions with equal areas. Write, but do not solve, an equation involving integral expressions whose solution gives the value $k$.


